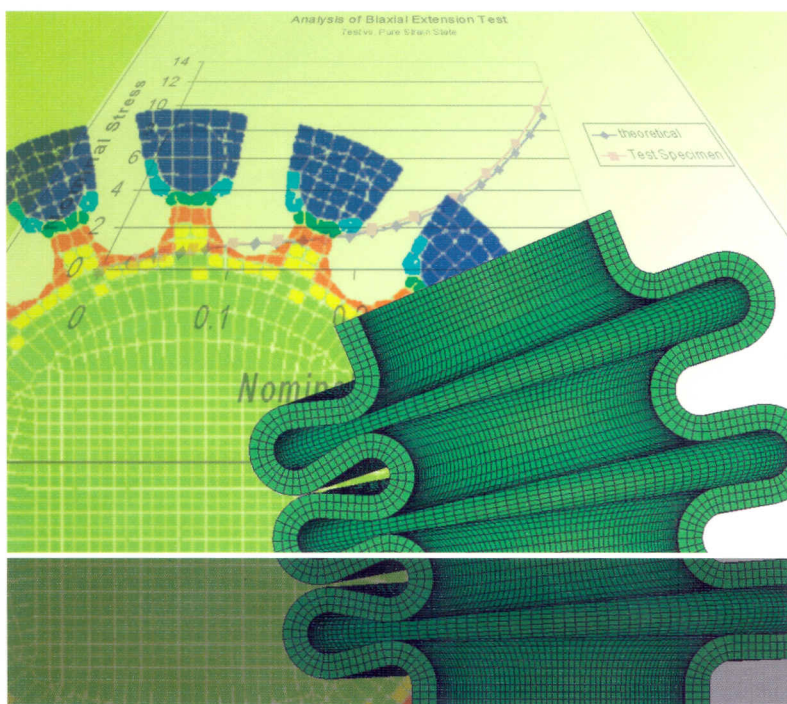


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Fatigue, Stress, and Strain of Rubber Components

Guide for Design Engineers



HANSER

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